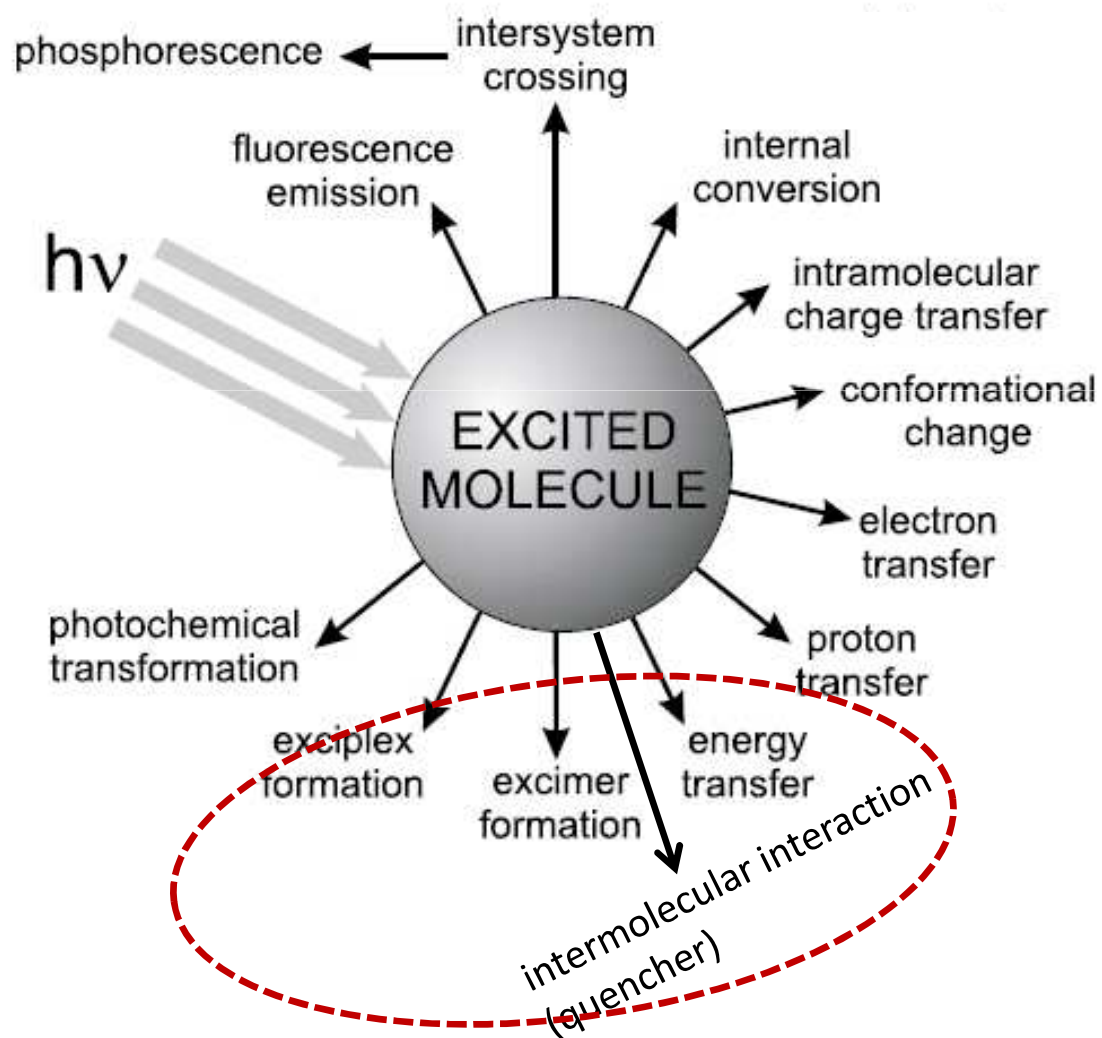
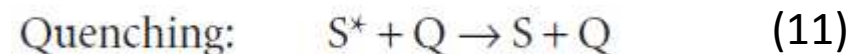
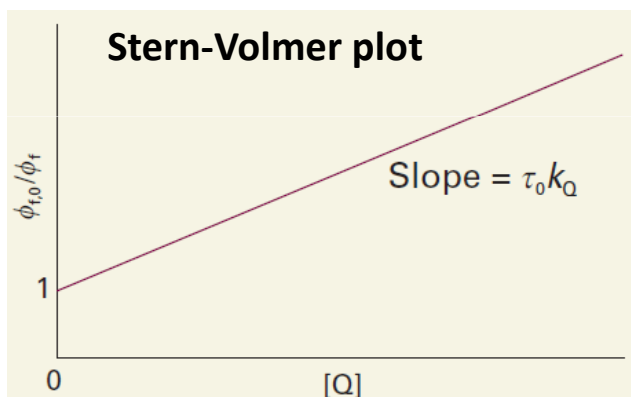
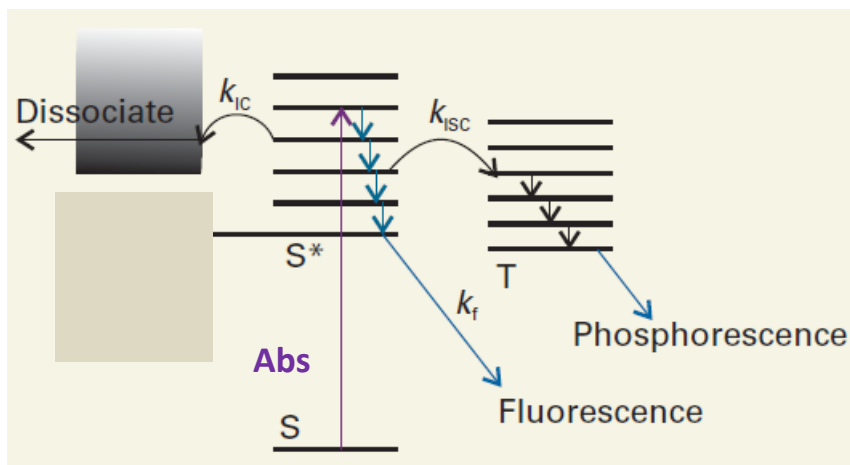


Pathways of decay of excited singlet states



Quenching



$$\frac{d[S^*]}{dt} = I_{\text{abs}} - (k_f + k_{\text{ISC}} + k_{\text{IC}} + k_Q[Q])[S^*] = 0 \quad (12)$$

The fluorescence quantum yield:

$$\phi_f = \frac{k_f}{k_f + k_{\text{ISC}} + k_{\text{IC}} + k_Q[Q]} \quad (13)$$

The quantum yield when $[Q] = 0$ is:

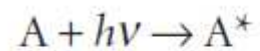
$$\phi_{f,0} = \frac{k_f}{k_f + k_{\text{ISC}} + k_{\text{IC}}} \quad (14)$$

$$\frac{\phi_{f,0}}{\phi_f} = \left(\frac{k_f}{k_f + k_{\text{ISC}} + k_{\text{IC}}} \right) \times \left(\frac{k_f + k_{\text{ISC}} + k_{\text{IC}} + k_Q[Q]}{k_f} \right) = 1 + \frac{k_Q}{k_f + k_{\text{ISC}} + k_{\text{IC}}}[Q]$$

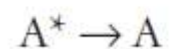
lifetime of excited singlet state $\tau_0 = \frac{1}{k_f + k_{\text{ISC}} + k_{\text{IC}}}$

The Stern–Volmer equation: $\frac{\phi_{f,0}}{\phi_f} = 1 + \tau_0 k_Q [Q]$ (15)

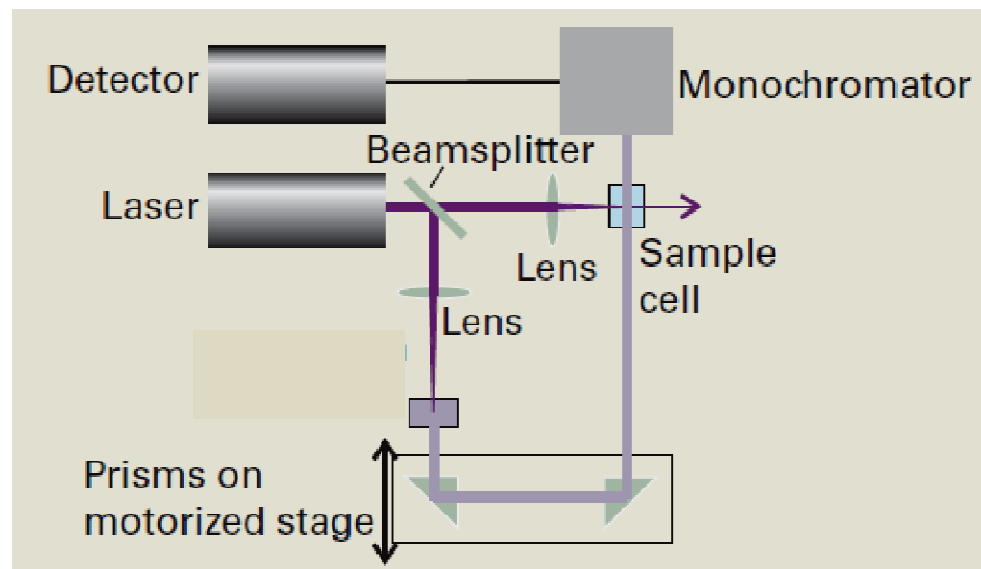
Determination of the lifetime of excited state (τ_0)



(absorption)



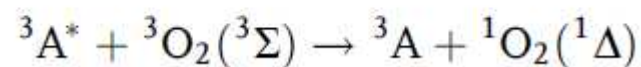
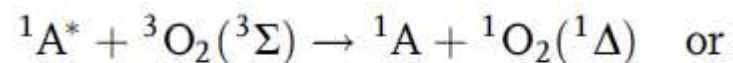
(emission)



O₂: well-known quencher of fluorescence

Ground state: $^3\Sigma$

Excited singlet states: $^1\Delta$ and $^1\Sigma$

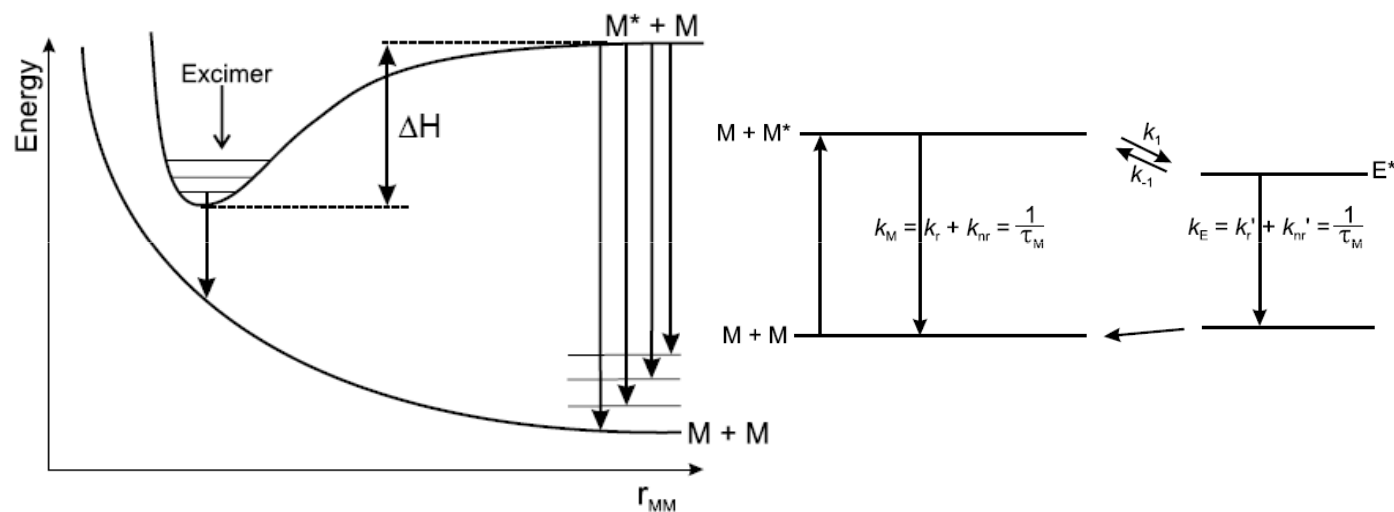
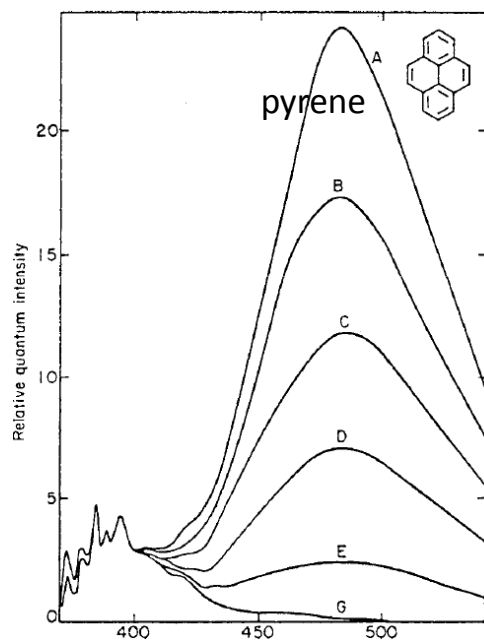


Excimer or Exciplex formation

Excimers : 'excited dimer'



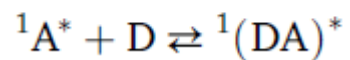
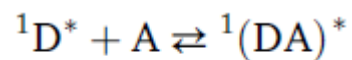
excitation energy is delocalized



Exciplexes : 'excited complex'

D = donor

A = acceptor

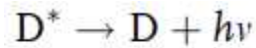


Excitation energy transfer



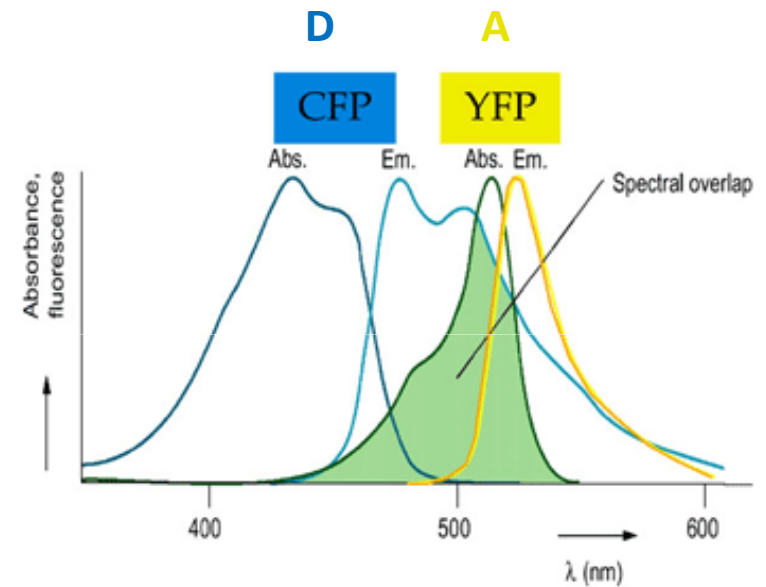
Radiative energy transfer:

- distances (D, A) larger than λ
- does not require any interaction between D and A
- depends on the spectral overlap and on the concentration

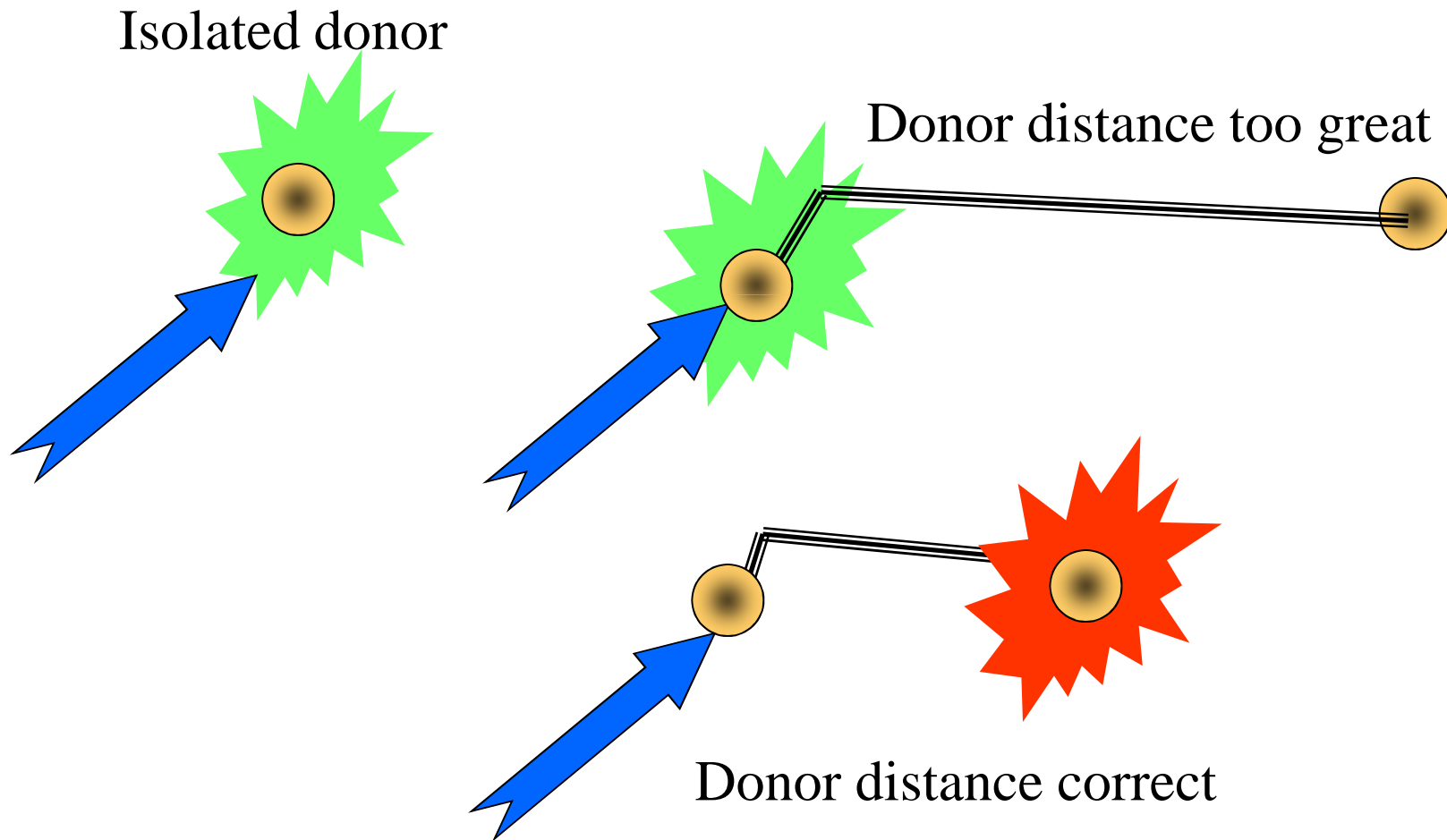


Non-radiative energy transfer:

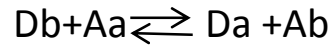
- distances (80-100 Å) less than the wavelength
- requires interactions between D and A (dipole-dipole)
- photosynthesis



- **Resonance energy transfer** can occur when the donor and acceptor molecules are less than 100 Å of one another (preferable 20-50 Å)



Fluorescence resonance energy transfer (FRET)



Calculate the rate at which the state of D,A changes from

$$\Psi_{D_b} \Psi_{A_a} \text{ to } \Psi_{D_a} \Psi_{A_b}$$

The rate of energy transfer

$$k_T(\nu) \propto |\langle \Psi_{D_a} \Psi_{A_b} | \tilde{V} | \Psi_{D_b} \Psi_{A_a} \rangle|^2$$

$$\tilde{V} = (\underline{\mu}_D \cdot \underline{\mu}_A) / R^3 - 3(\underline{\mu}_D \cdot \mathbf{R})(\mathbf{R} \cdot \underline{\mu}_A) / R^5$$

$$\tilde{V} = \kappa |\underline{\mu}_D| |\underline{\mu}_A| / R^3$$

κ geometry parameter

With (17) in (16):

$$k_T(\nu) \propto |(\kappa/R^3) \langle \Psi_{D_a} \Psi_{A_b} | \underline{\mu}_D | \underline{\mu}_A | \Psi_{D_b} \Psi_{A_a} \rangle|^2$$

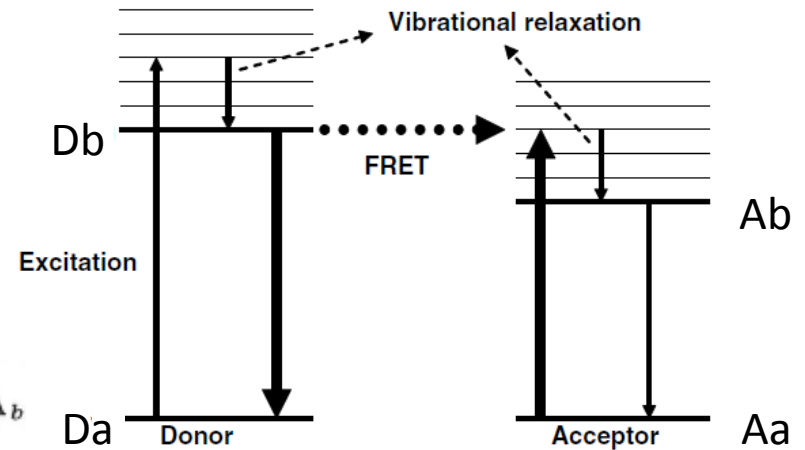
$$k_T(\nu) \propto (\kappa^2/R^6) |\langle \Psi_{D_a} | \underline{\mu}_D | \Psi_{D_b} \rangle|^2 |\langle \Psi_{A_b} | \underline{\mu}_A | \Psi_{A_a} \rangle|^2$$

Absorption takes place at a single frequency ν :

$$|\langle \Psi_{A_b} | \underline{\mu}_A | \Psi_{A_a} \rangle|^2 \propto \epsilon_A \nu^{-1}$$

$$D_{ab} \propto \nu^{-3} A_{ba} = \nu^{-3} \tau_S^{-1}$$

$$\tau_S^{-1} = \phi_D / \tau_D \quad \longrightarrow \quad |\langle \Psi_{D_a} | \underline{\mu}_D | \Psi_{D_b} \rangle|^2 \propto \nu^{-3} \phi_D / \tau_D$$



(16)

(17)

FRET

The energy transfer rate: $k_T(\nu) \propto (\kappa^2/R^6)(\phi_D/\tau_D)\epsilon_A\nu^{-4}$

Fluorescence of D and absorption of A occur over a range of frequencies:

$$k_T \propto (\kappa^2/R^6)(\phi_D/\tau_D) \int \epsilon_A(\nu) f_D(\nu) \nu^{-4} d\nu = (\kappa^2 \phi_D / R^6 \tau_D) J$$

In a fluid medium, the true interaction potential is V/n^2
 n is the refractive index

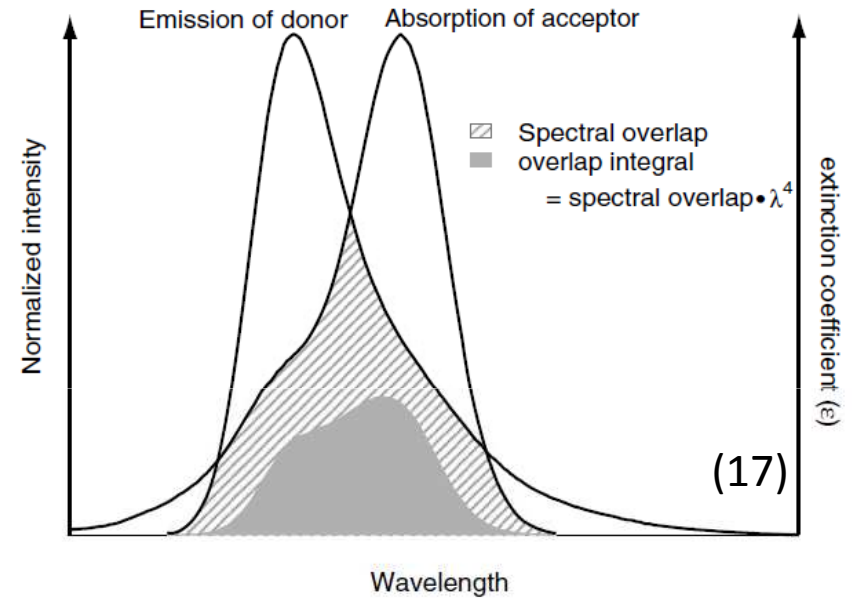
Förster radius $R_0^6 = 8.79 \times 10^{-5} \cdot \frac{\Phi_D \cdot \kappa^2 \cdot J}{n^4} \text{ cm}^6$

; The distance at which 50% energy transfer takes place

The energy transfer rate: $k_T = (R_0/R)^6 \tau_D^{-1}$ (18)

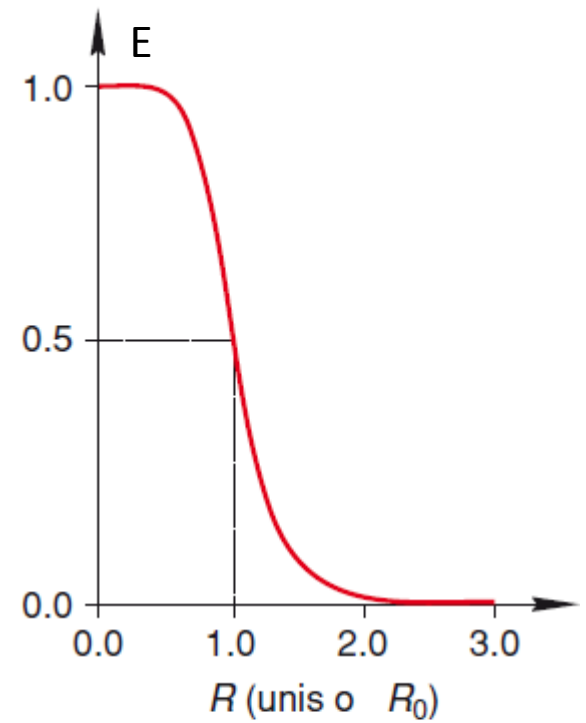
FRET efficiency E: $E = k_T / (k_T + \tau_D^{-1})$ (19)

$$E = \frac{R_0^6}{R_0^6 + R^6} \quad (20)$$

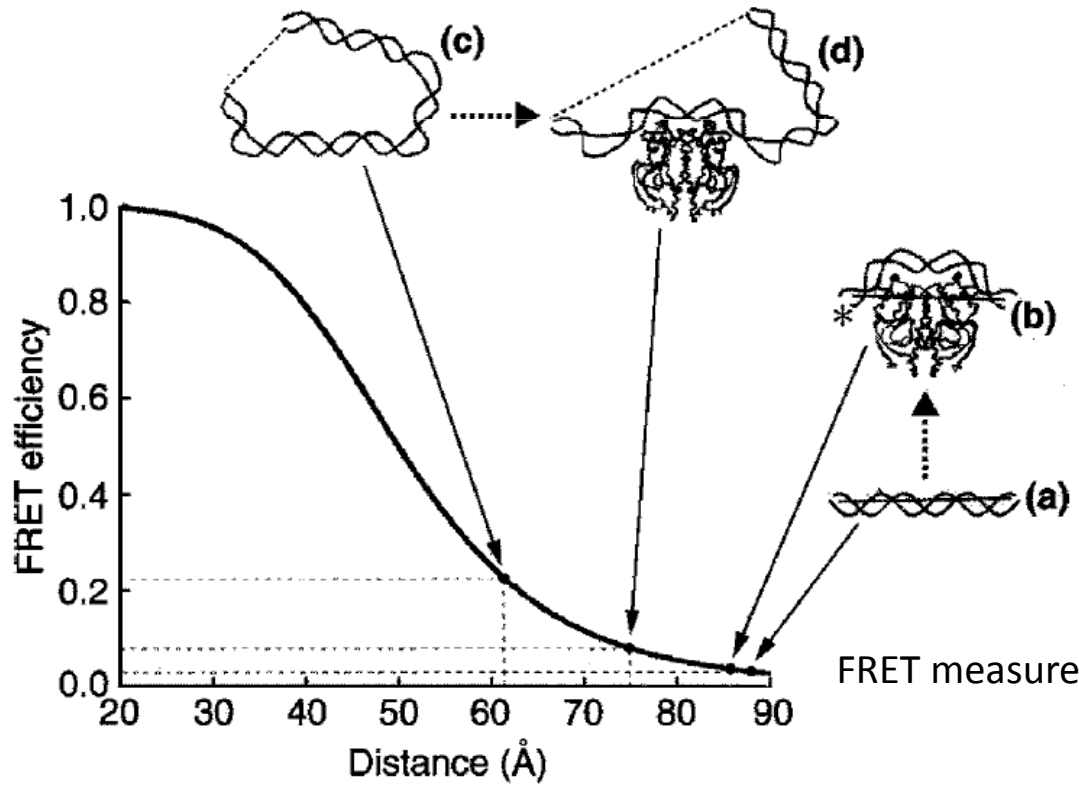


$$E = \frac{R_0^6}{R_0^6 + R^6} \quad (20) \quad \text{spectroscopic ruler in the range } 10\text{-}100 \text{ \AA}$$

k^2 : relative orientation of the transition dipoles of D and A.
 = 2/3 isotropic dynamic average

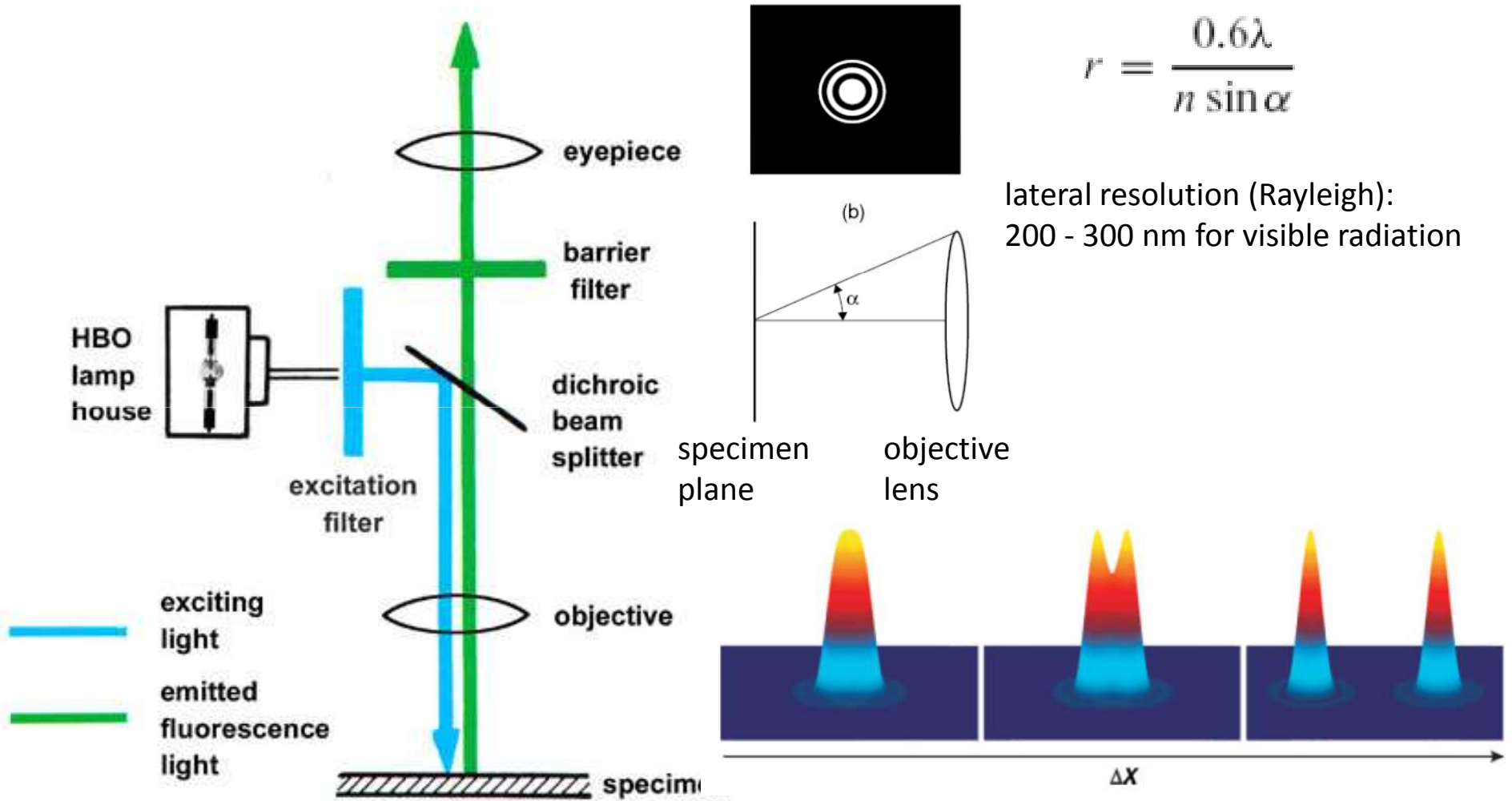


$$0.5R_0 < R < 1.5R_0$$



FRET measures distances in proteins

Fluorescence microscopy

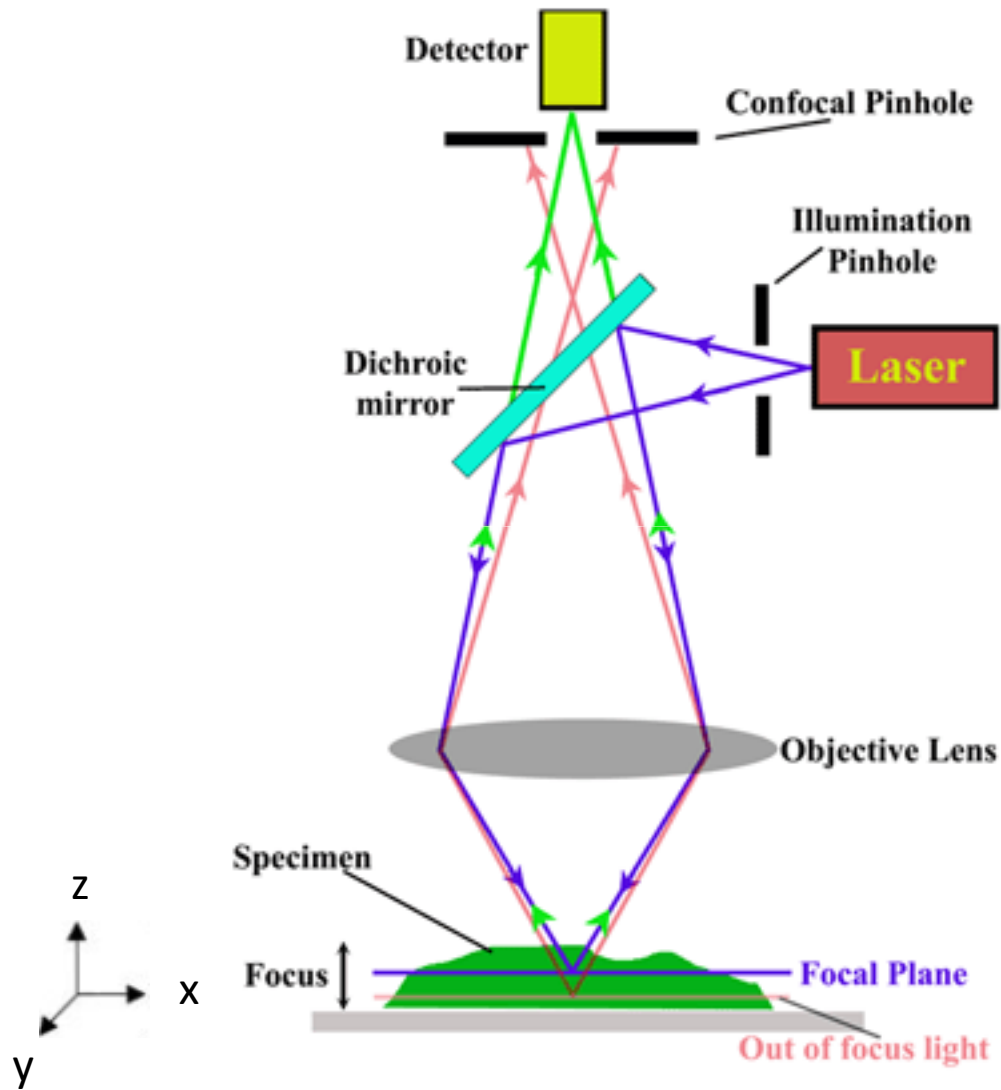


$$r = \frac{0.6\lambda}{n \sin \alpha}$$

lateral resolution (Rayleigh):
200 - 300 nm for visible radiation

axial resolution: 700 nm

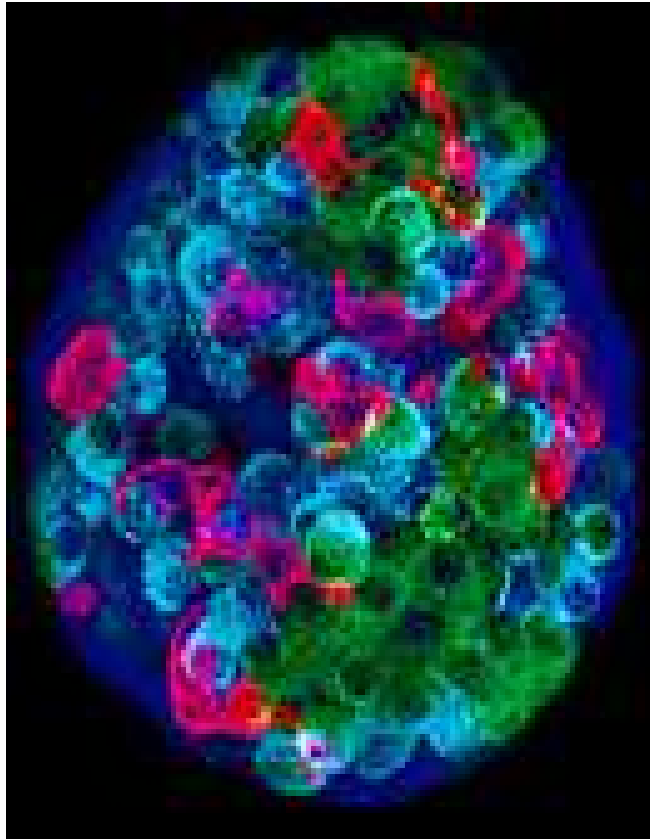
Fluorescence confocal microscopy: 3D images



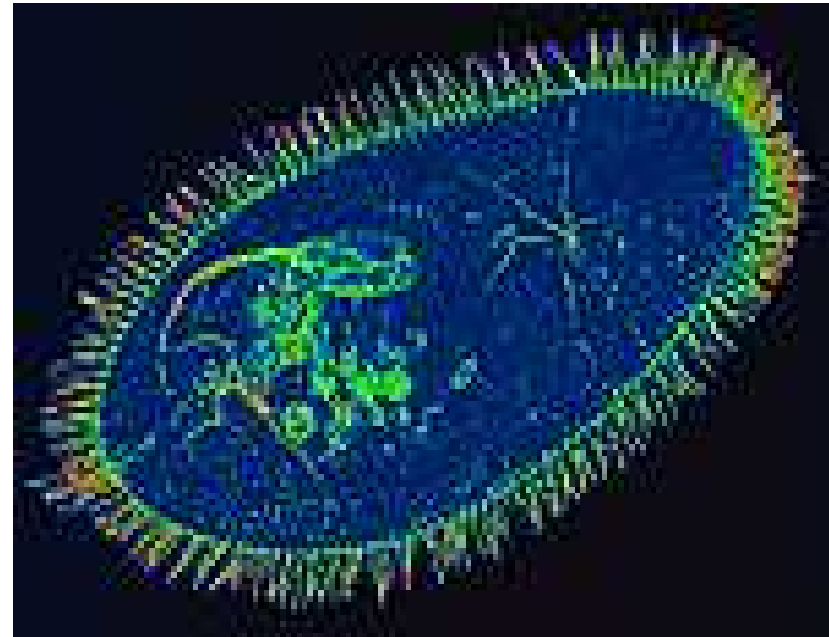
Advantage of confocal microscopy:
optical sectioning: 3D images of specimens

Disadvantage:
higher amount of photobleaching

Applications

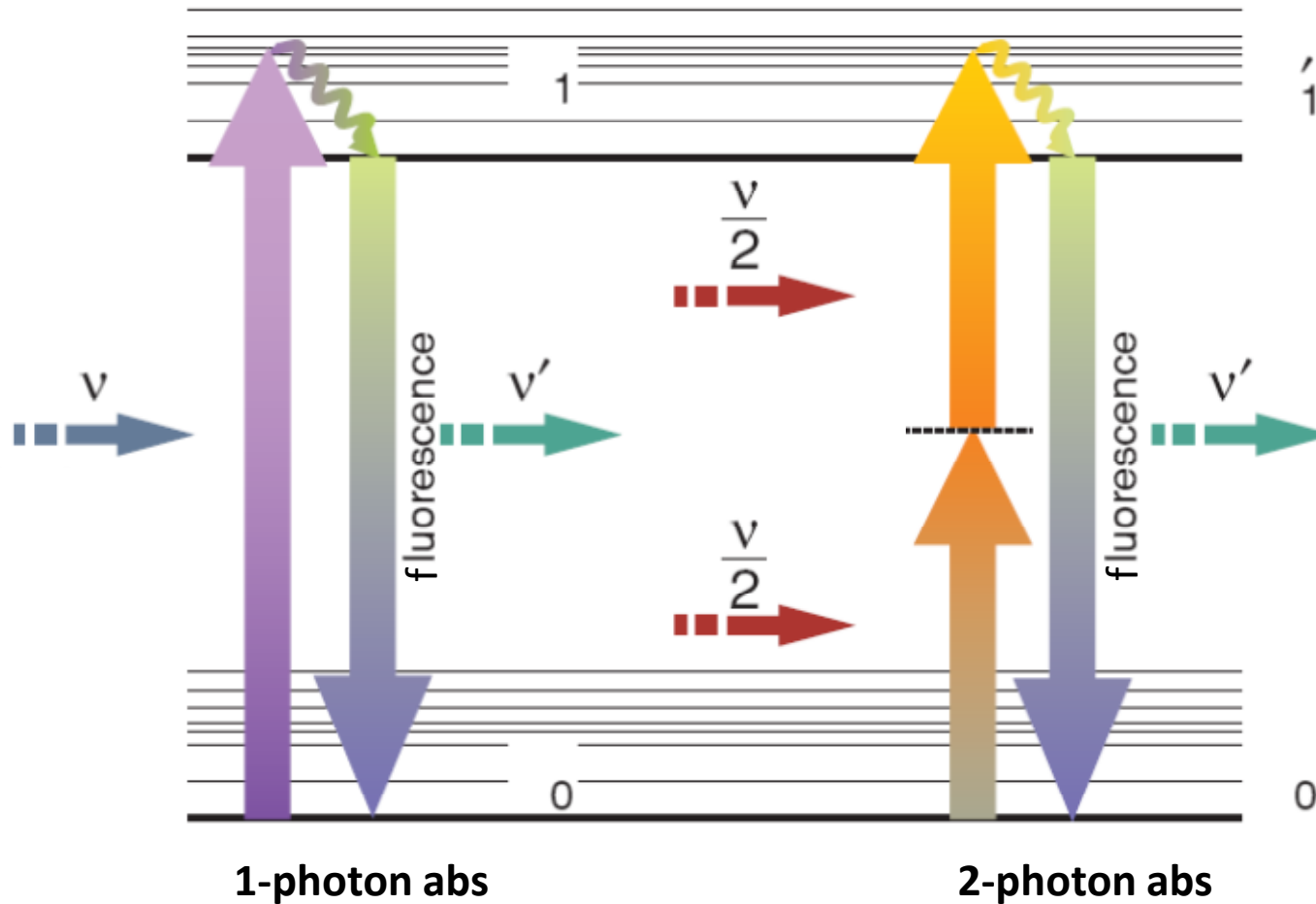


Projection of 25 optical sections of a triple-labeled rat islet of Langerhans, acquired with a krypton/argon laser.



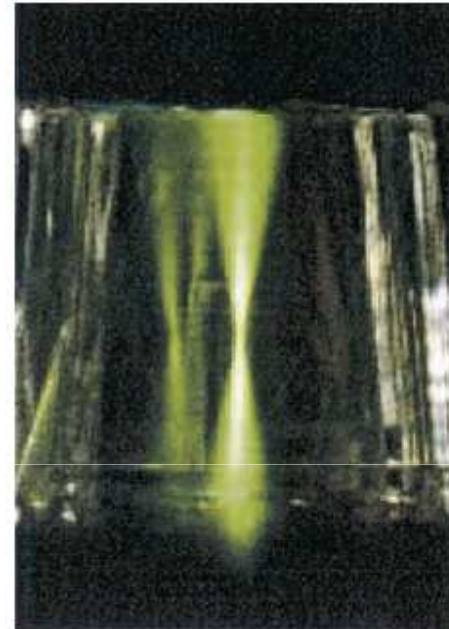
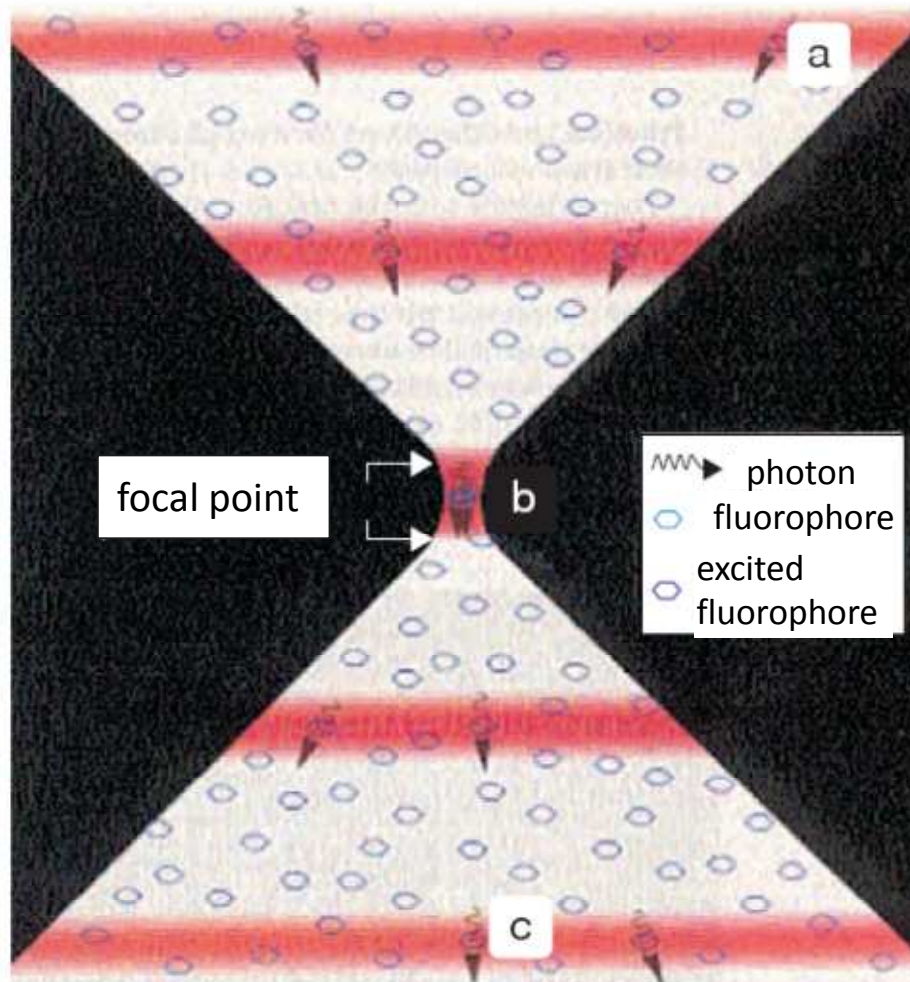
Paramecium: thousands of cilia and internal microtubular structures.

Two-photon excitation fluorescence microscopy: 3D images



The cross-sections for two-photon absorption: $10^{-50} \text{ cm}^4 \text{ s photon}^{-1} \text{ molecule}^{-1}$ (rhodamine B).
Used lasers: *Titan:Sapphire laser (TiSa)*

Two-photon excitation fluorescence microscopy: 3D images



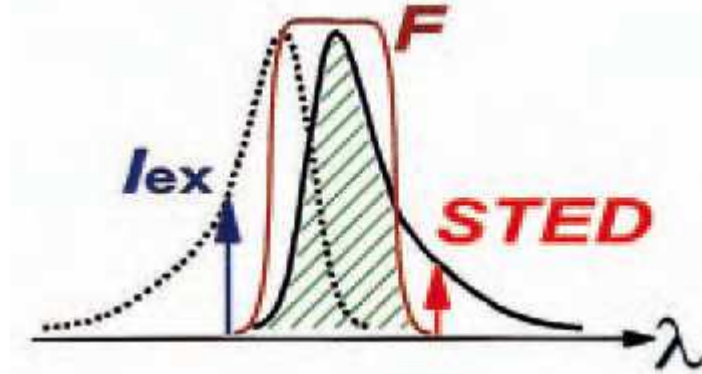
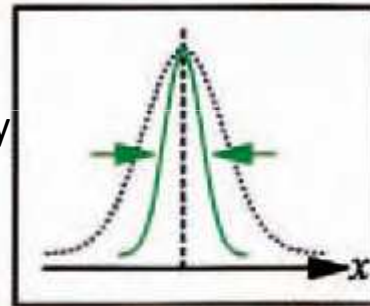
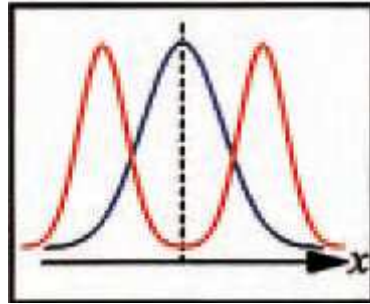
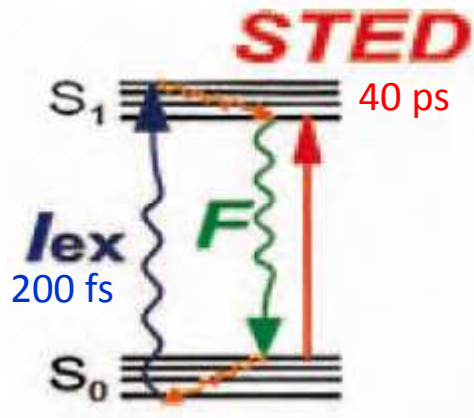
Advantages:

- no out-of-focus photobleaching
- excitation beam is not attenuated by out-of-focus absorption, (increased penetration depth)

Disadvantage:

- lower spatial resolution than in confocal imaging (longer wavelength!)

Stimulated emission depletion (STED) microscopy: resolution beyond the Rayleigh limit

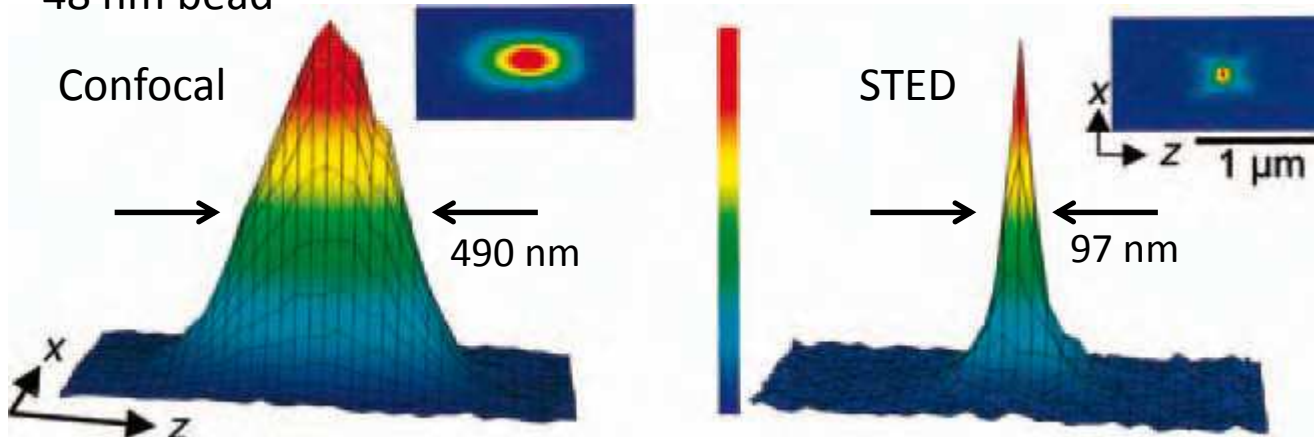


$$\Delta x \approx \frac{\lambda}{2n \sin \alpha \sqrt{1 + I/I_{\text{sat}}}}$$

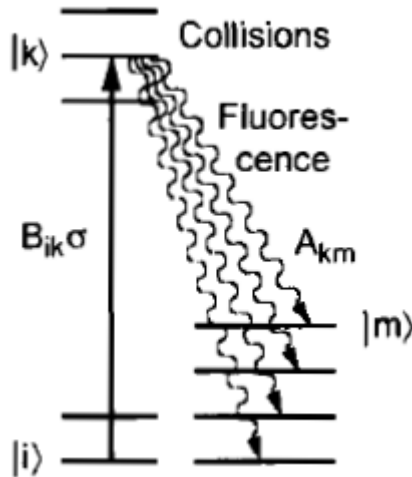
I_{sat} : intensity at which the fractional population of the excited state is depleted to $1/e$
 30 MW cm^{-2} in the visible range

The fluorescence is confined spatially to sub-diffraction dimensions

48 nm bead



Laser induced fluorescence



The number of photons absorbed per second along the path length Δx : $n_a = N_i n_L \sigma_{ik} \Delta x$

n_L : number of incident laser photons per second

σ_{ik} : absorption cross section per molecule

N_i : density of molecules in the absorbing state i

The number of fluorescence photons emitted per second from the excited level:

$$n_{F1} = N_k A_k = n_a \eta_k$$

η_k quantum efficiency of the excited state

The number n_{pe} of photoelectrons counted per second:

$$n_{pe} = n_a \eta_k \eta_{ph} \delta = (N_i \sigma_{ik} n_L \Delta x) \eta_k \eta_{ph} \delta$$

$$\delta = d\Omega / 4\pi$$

η_{ph} quantum efficiency of the photocathode (0.2)

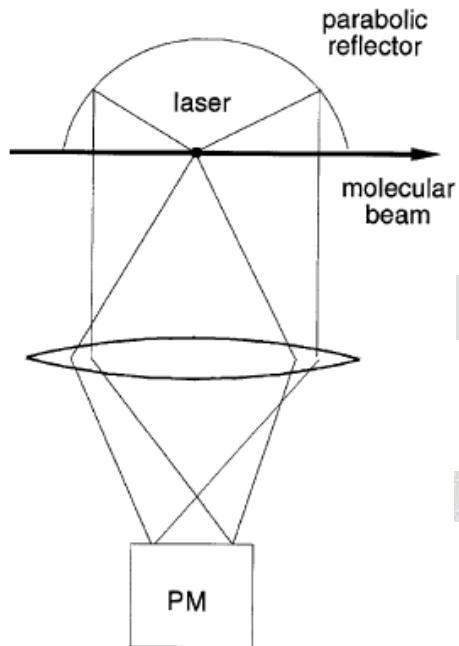
Ex:

$$\eta_{ph} = 0.2 \quad \delta = 0.1 \quad d\Omega = 0.4 \pi \quad n_{pe} = 100 \text{ counts/s} \quad \eta_k = 1$$

$$n_a = 5 \times 10^3 /s$$

$$\text{laser power of 1 W at the wavelength } \lambda = 500 \text{ nm} \quad n_L = 3 \times 10^{18} /s$$

$$(I_0 - I_{trans}) / I_0 = 10^{-15}$$



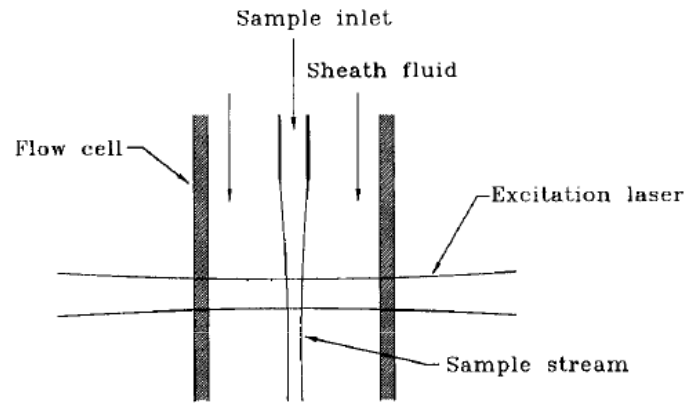
Single molecule detection

spontaneous lifetime τ : 10^{-8} s

travel time T through the laser beam: 10^{-5} s

excitation-fluorescence cycles $n = T/\tau$: 500 photons / molec

➡ single molecule detection



(a)

